

Definitions / Assumptions

Homojunction: the junction is between two regions of the same material **Heterojunction**: the junction is between two different semiconductors

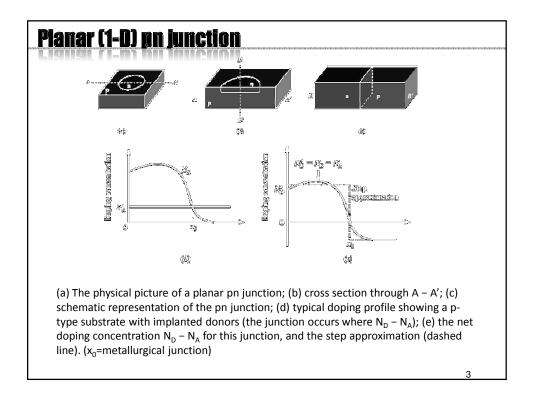
Approximations used in the step-junction model

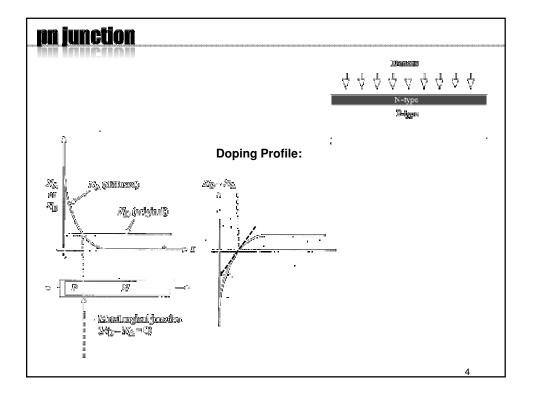
1. The doping profile is a step function. On the n-type side, $N'_D = N_D - N_A$ and is constant. On the p side, $N'_A = N_A - N_D$ and is constant.

2. All impurities are ionized. Thus the equilibrium electron concentration on the n side is

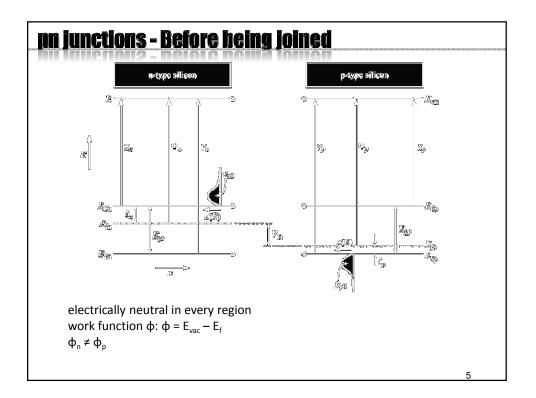
 $n_{n0} = N'_{D}$. The equilibrium hole concentration on the p side is $p_{p0} = N'_{A}$.

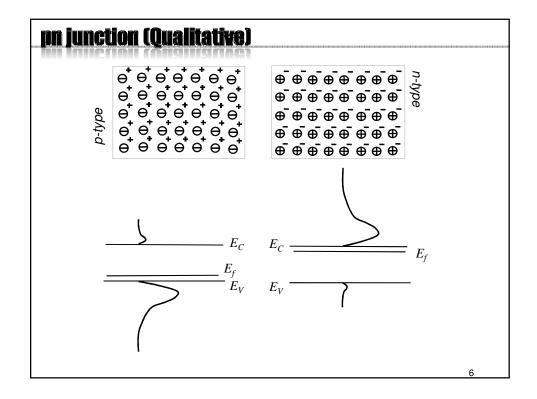
3. Impurity-induced band-gap narrowing effects are neglected.

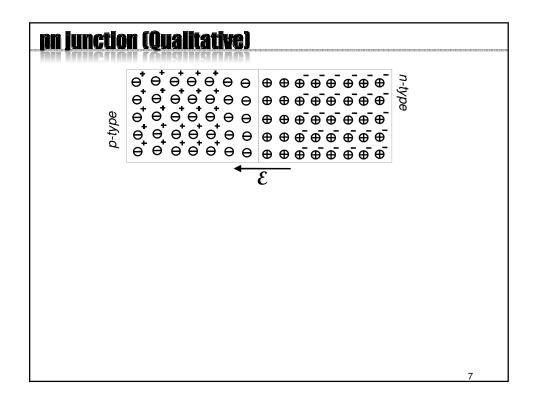


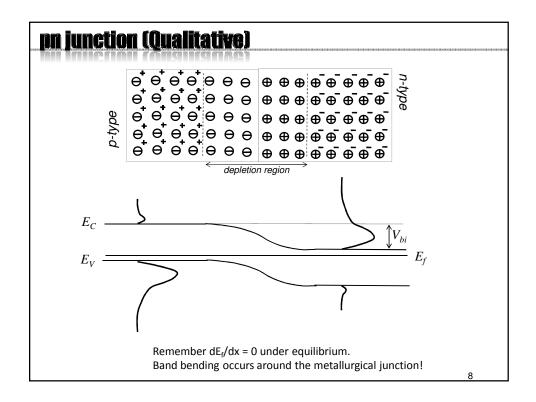


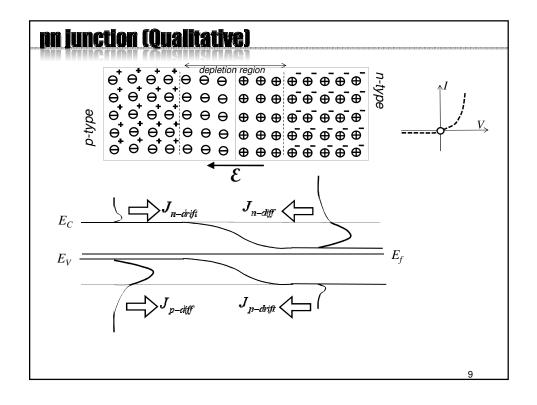
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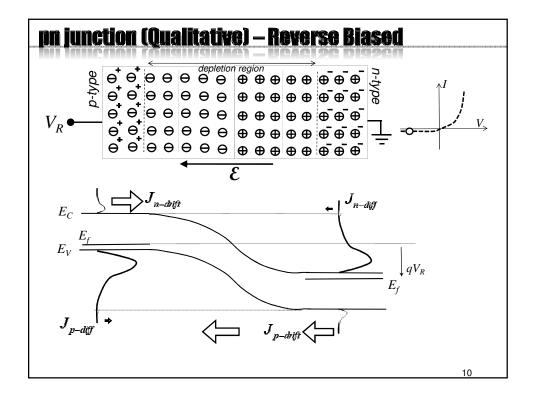


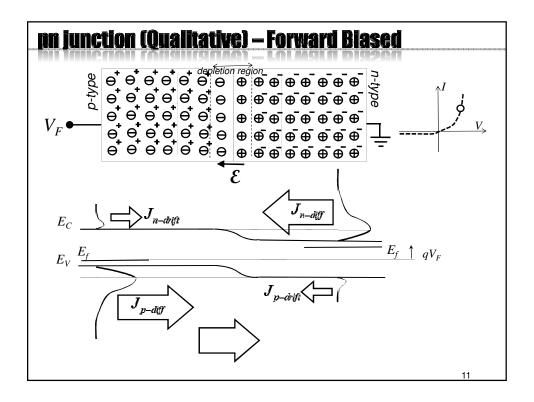


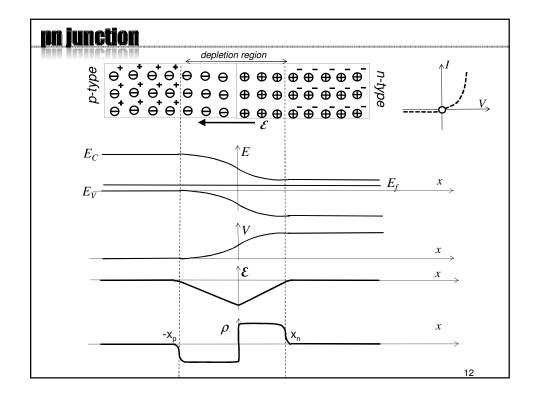




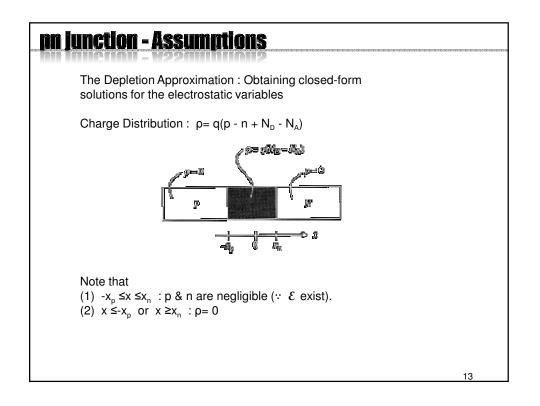


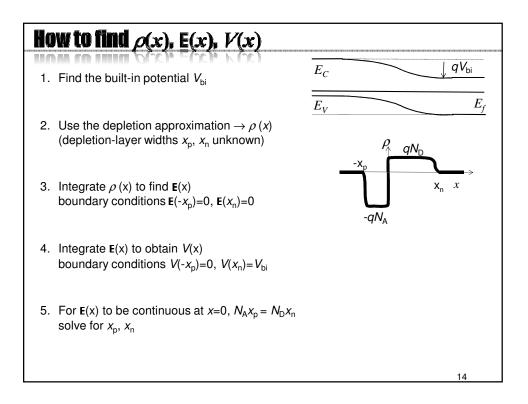




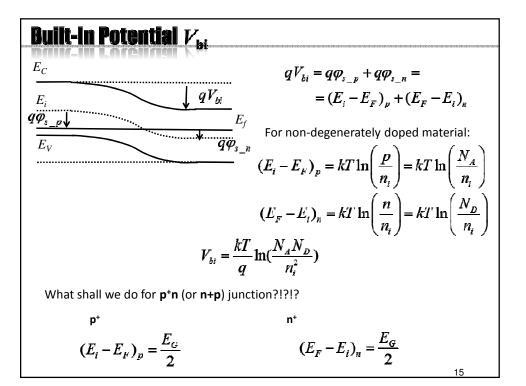


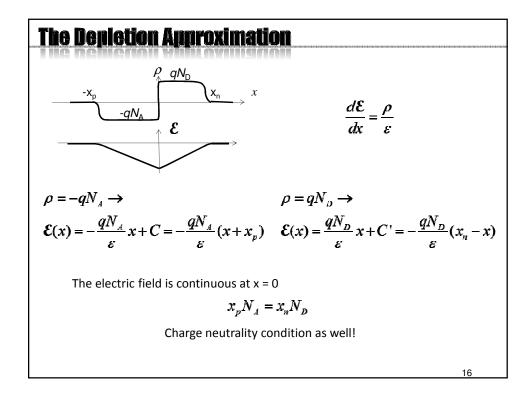
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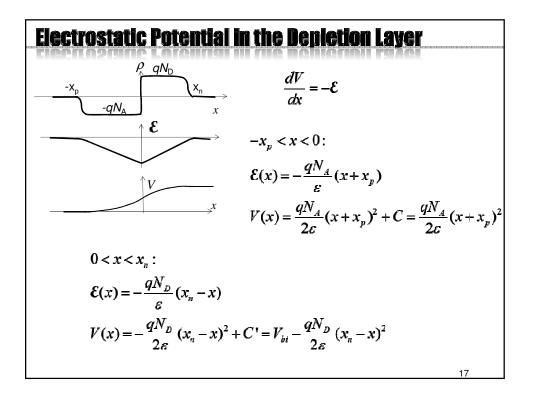




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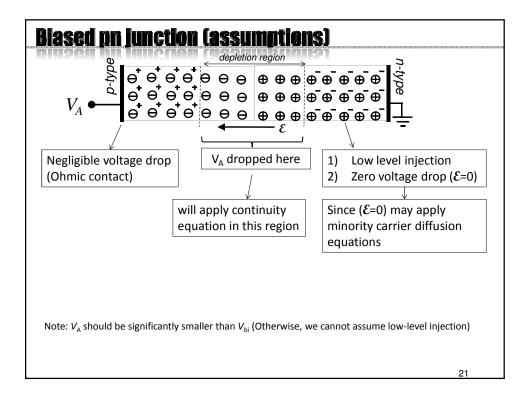


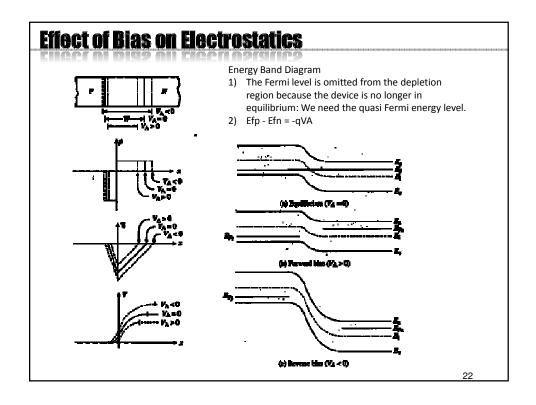


Depletion Layer Width If $N_A >> N_D$ as in a p⁺n junction: $\begin{aligned} W &= \sqrt{\frac{2\varepsilon_s V_{bt}}{q}} \left(\frac{1}{N_A} + \frac{1}{N_D}\right) \rightarrow W = \sqrt{\frac{2\varepsilon_s V_{bt}}{qN_D}} \approx x_n \\ x_p N_A &= x_n N_D \rightarrow x_p \ll x_n \rightarrow x_p \approx 0 \end{aligned}$ Note: $V_{bi} &= \frac{E_G}{2q} + \frac{kT}{q} \ln \frac{N_D}{n_i}$ 19

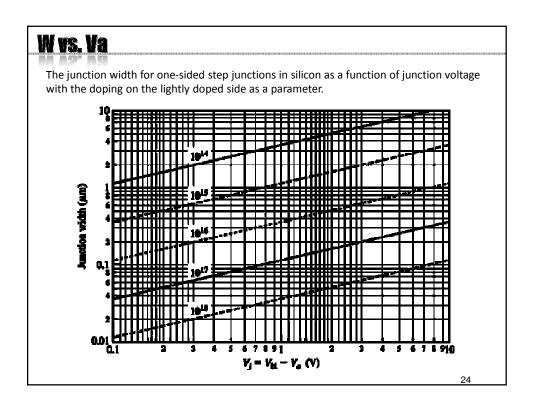
Example
A p⁺n junction has N_A=10²⁰ cm⁻³ and N_D=10¹⁷cm⁻³. What is
a) its built in potential,
$$V_{bi} = \frac{E_G}{2q} + \frac{kT}{q} \ln \frac{N_D}{n_i} \approx 1 \text{ V}$$

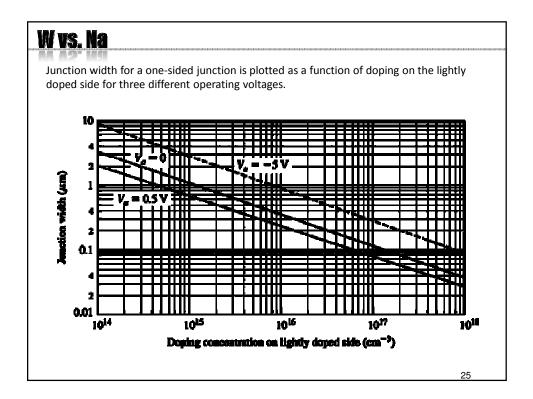
b) W, $W \approx \sqrt{\frac{2\varepsilon_s V_{bi}}{qN_D}} = \left(\frac{2 \times 12 \times 8.85 \times 10^{-14} \times 1}{1.6 \times 10^{-19} \times 10^{17}}\right)^{1/2} = 0.12 \text{ µm}$
c) x_n , and $x_n \approx W = 0.12 \text{ µm}$
d) $x_p = x_n N_D / N_A = 1.2 \times 10^{-4} \text{ µm} = 1.2 \text{ Å} \approx 0$



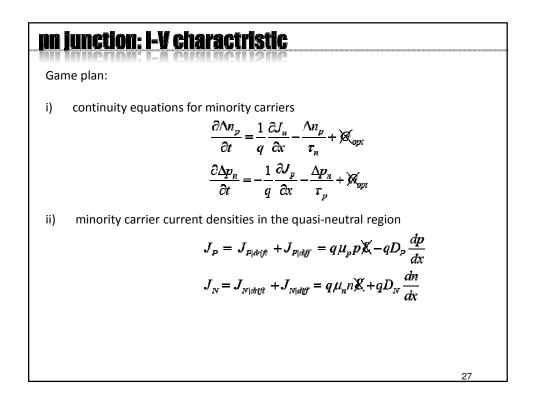


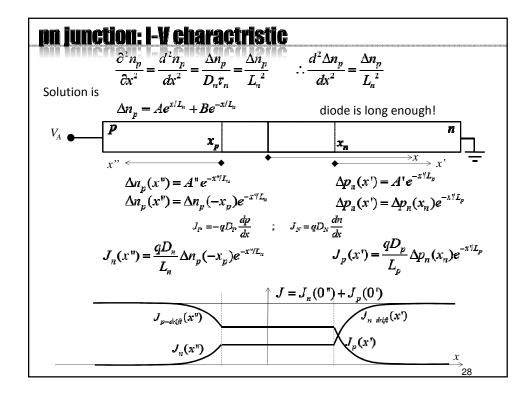
EXAMPLIED VOLTAGE Now as we assumed all voltage drop is in the depletion region (Note that VA < Vbi) $\kappa_{\mu} + \kappa_{\mu} = W = \sqrt{\frac{2\varepsilon_{\mu}(V_{be} - V_{A})}{q} \left(\frac{1}{N_{A}} + \frac{1}{N_{D}}\right)}$ $\kappa_{\mu} N_{A} = \kappa_{\mu} N_{D}$



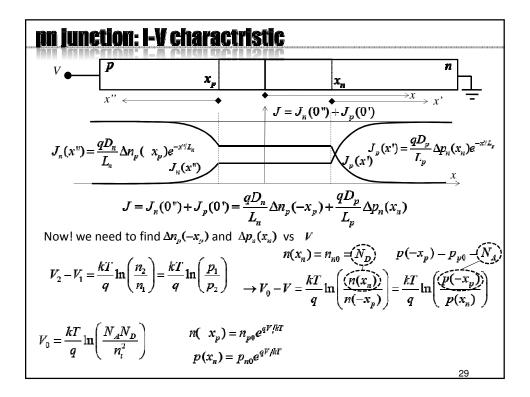


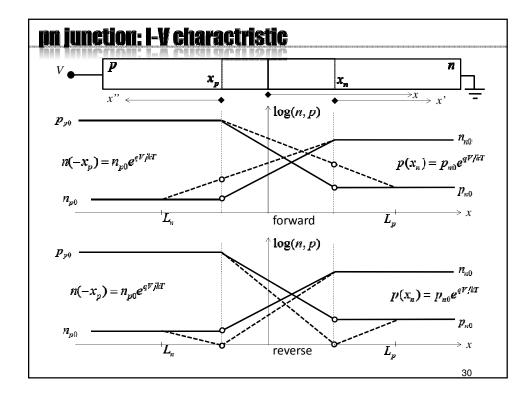
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Assumption:
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1) Δνα-level injection: η_ρ ≪ ρ_ρ ~ Λ_α (or Λn ≪ ρ_ρ, ρ ~ ρ_ρ in p-type) β_n α α_n ~ Λ_D (or Δρ ≪ α₀, σ, σ₀ in n-type)
2) In the bulk, η_n ~ η_nθ = Λ_D , ρ_ρ ~ ρ_ρθ = Λ_d
3) For minority carriers δ_{evif} ≪ δ_{dif} in quasi-neutral regions
4) Nondegenerately doped step junction
5) Long-base diode in 1-D (both sides of quasi-neutral regions are much longer than their minority carrier diffusion lengths, Ln or Lp)
6) No Generation/Recombination in depletion region
7) Steady state δ/df = θ
8) Gopt = 0



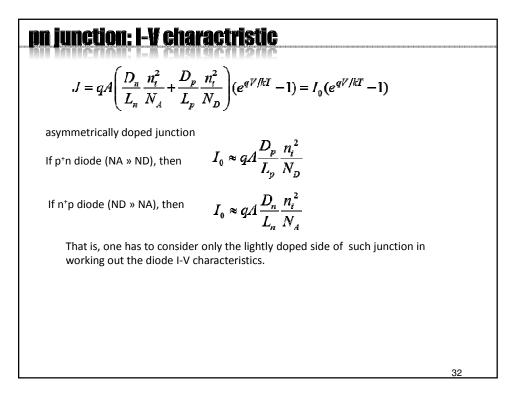


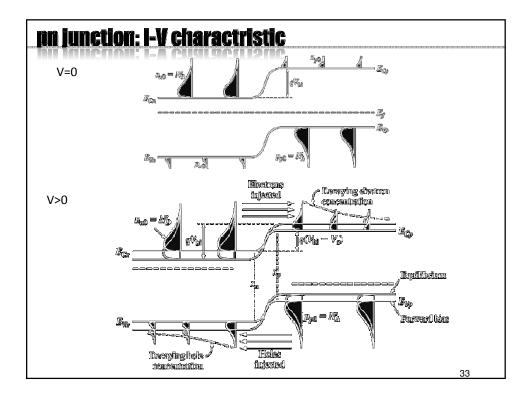
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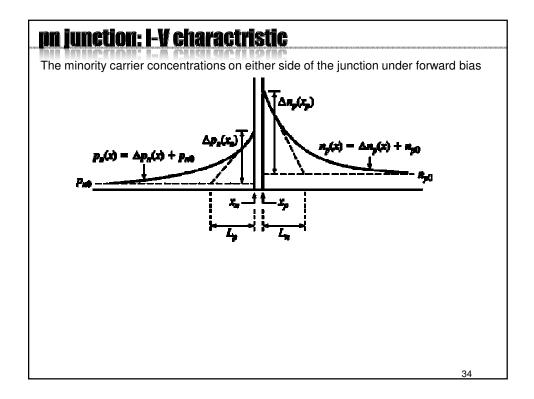


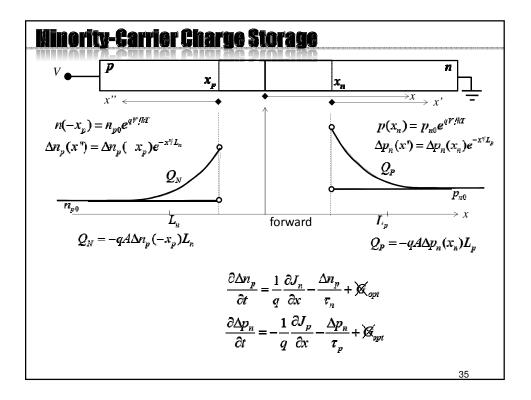


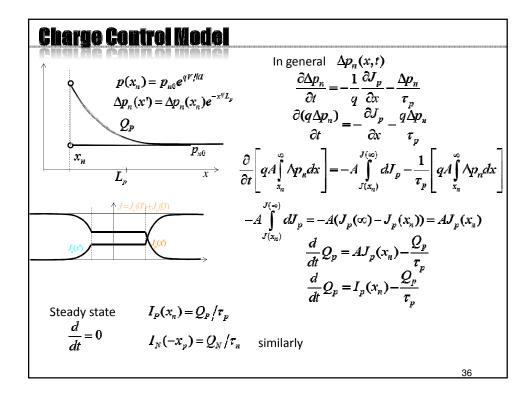
$\begin{aligned} \textbf{m junction: I-V charactristic} \\ J = J_n(0^n) + J_p(0^n) &= \frac{qD_n}{L_n} \wedge n_p(-x_p) + \frac{qD_p}{L_p} \wedge p_n(x_n) \\ n(-x_p) &= n_{p0} e^{qV/kT} \\ \Delta n_p(-x_p) &= n - n_{p0} = n_{p0} (e^{qV/kT} - 1) \\ n_{p0} &= n_i^2/N_A \end{aligned}$ $\begin{aligned} p(x_n) &= p_{n0} e^{qV/kT} \\ \Delta p_n(x_n) &= p - p_{n0} = p_{n0} (e^{qV/kT} - 1) \\ J &= q \left(\frac{D_n}{L_n} n_{p0} + \frac{D_p}{L_p} p_{n0} \right) (e^{qV/kT} - 1) \\ I &= AJ \end{aligned}$ $\begin{aligned} J &= qA \left(\frac{D_n}{L_n} \frac{n_i^2}{N_A} + \frac{D_p}{L_p} \frac{n_i^2}{N_D} \right) (e^{qV/kT} - 1) = I_0 (e^{qV/kT} - 1) \\ I_0 &= qA n_i^2 \left(\sqrt{\frac{D_n}{\tau_n}} \frac{1}{N_A} + \sqrt{\frac{D_p}{\tau_p}} \frac{1}{N_D} \right) \end{aligned}$

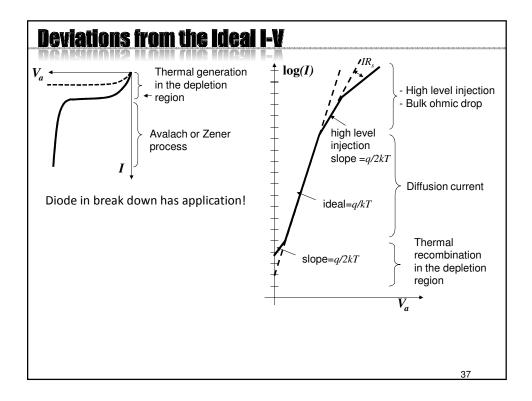


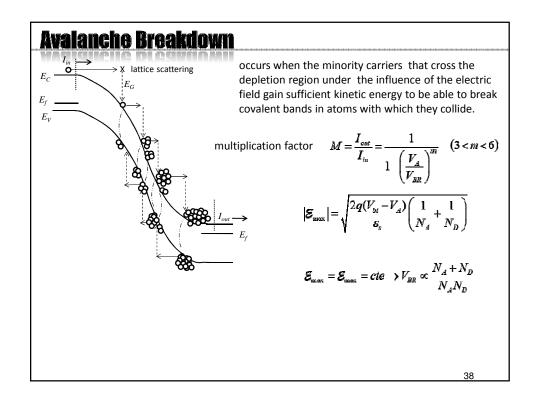


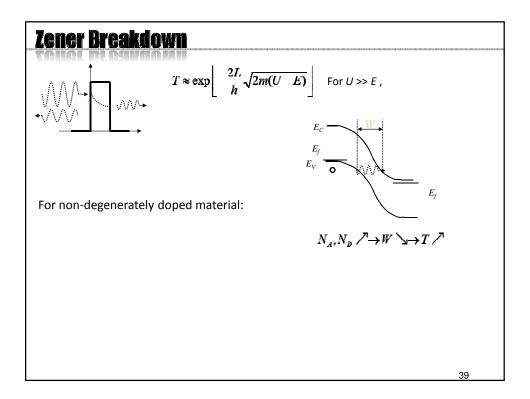


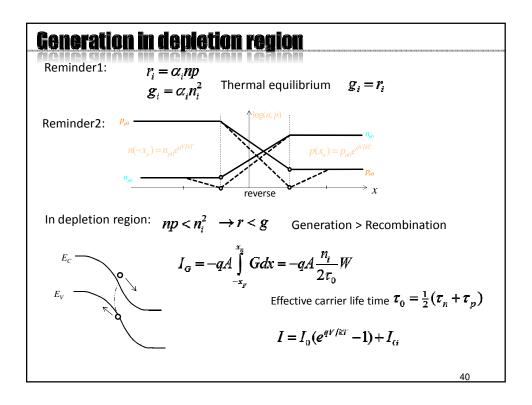


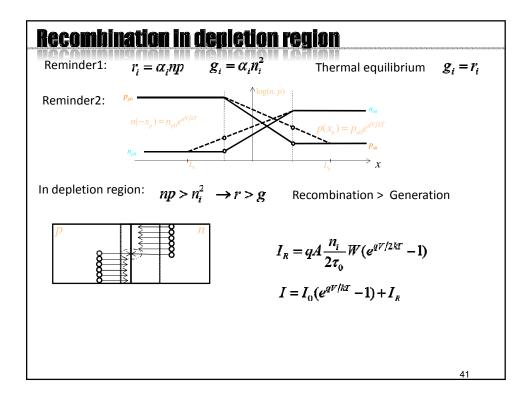


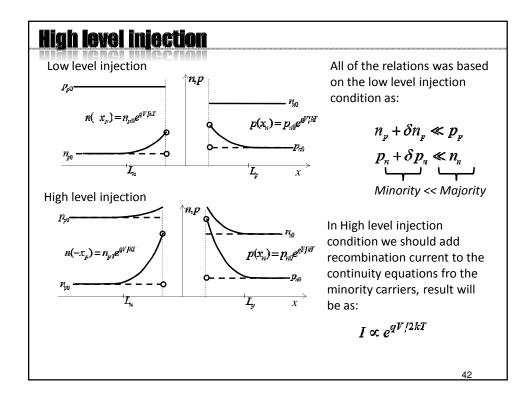


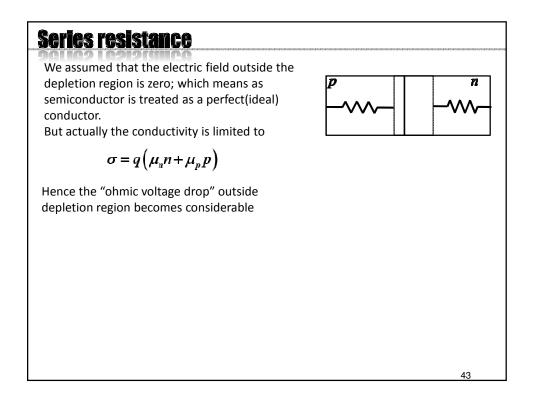


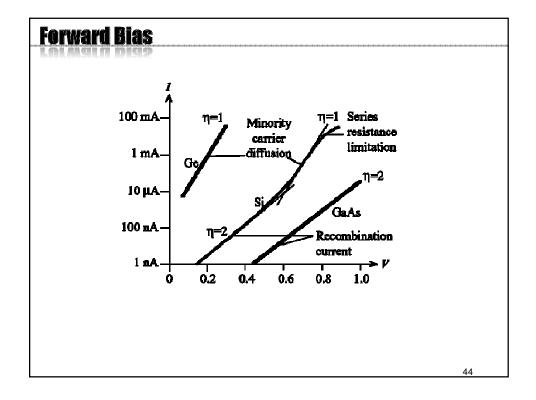


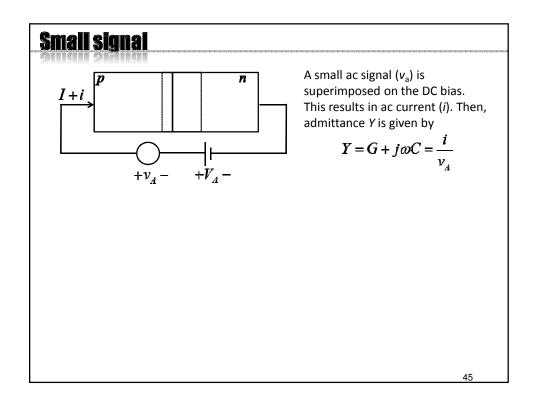


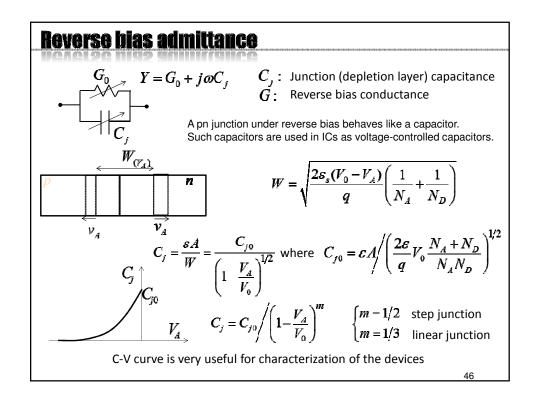


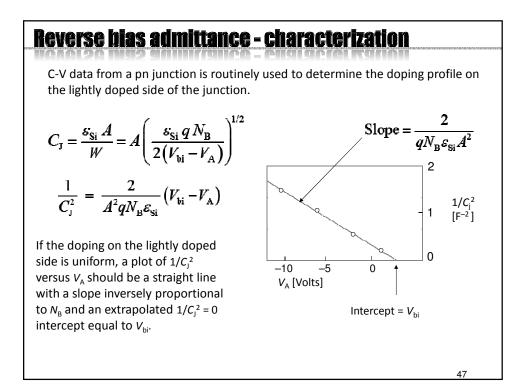


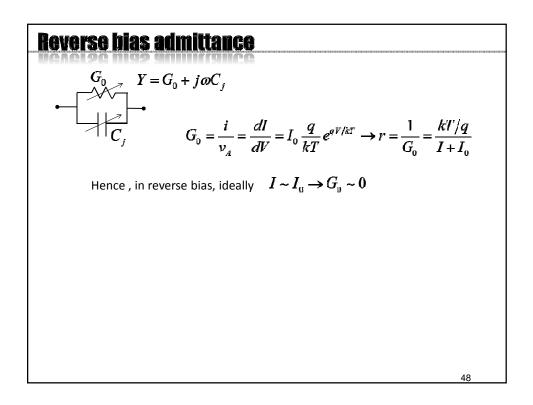


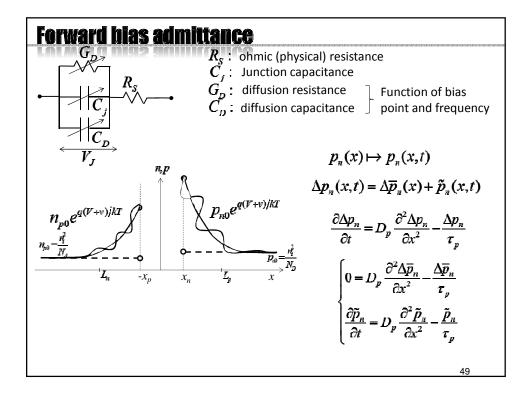




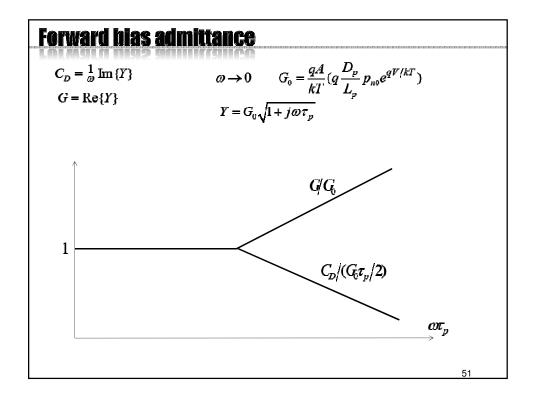


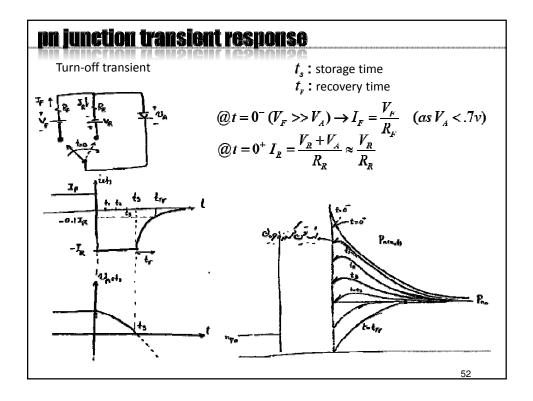






Forward hias admittance
$\frac{\partial \tilde{p}_n}{\partial t} = D_p \frac{\partial^2 \tilde{p}_n}{\partial x^2} - \frac{\tilde{p}_n}{\tau_p} \text{Phasor representation} \tilde{p}_n(x,t) = \hat{p}_n(x)e^{j\alpha t}$
$\frac{d^2 \hat{p}_n}{dx^2} = \hat{p}_n (\frac{1+j\omega t}{D_p \tau_p}) = \frac{\hat{p}_n}{L_p^{*2}} \text{ where } L_p^{*2} = \frac{L_p^2}{1+j\omega \tau_p}$
$\hat{p}_n(x) = \mathbb{X}_1 e^{x/L_p^*} + B_2 e^{-x/L_p^*}$
$ \hat{p}_{n}(x) = \mathbb{X}_{1} e^{x/L_{p}} + B_{2} e^{-x/L_{p}} p_{n}(0,t) = p_{n0} e^{q(V+v(t))/kT} \approx p_{n0} e^{qV/kT} \left(1 + \frac{qv(t)}{kT}\right) $ $ B_{2} = p_{n0} e^{qV/kT} \frac{qv}{kT} $
$i = -qAD_{\nu} \left. \frac{d\hat{p}_n}{dx} \right _{x=0} = qA \frac{D_{\nu}}{L_{\nu}^*} p_{n0} e^{q\nu/kT} \frac{q\nu}{kT}$
$Y = \frac{i}{v} = A \frac{q}{kT} (q \frac{D_p}{L_p^*} p_{n0}) e^{qV/kT} = A \frac{q}{kT} (q \frac{D_p}{L_p} p_{n0} \sqrt{1 + j\omega\tau_p}) e^{qV/kT}$
$\operatorname{Re}\{\}= \frac{G}{G} \qquad \operatorname{Im}\{\}= \frac{\partial C}{\partial C}$
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charge control for p+n diode $\frac{dQ_p(t)}{dt} = i(t) - \frac{Q_p(t)}{\tau_p}$
$dt = \tau(t)$
i i p
for $0 < t < t_s$: $i(t) = -I_R$
$\frac{dQ_p(t)}{dt} = -I_R - \frac{Q_p(t)}{\tau_p} \to \int_{Q_p(0^-)}^{Q_p(t_p) \to 0} \frac{dQ_p}{I_R + \frac{Q_p(t)}{\tau_p}} = -\int_0^{t_p} dt = -t_s = -\tau_p \ln(1 + \frac{Q_p(0^+)}{I_R \tau_p})$
but for $t = 0^-$: $\frac{dQ_p}{dt} = 0 = I_F - \frac{Q_p(0^-)}{\tau_p} \to Q_p(0^-) = I_F \tau_p = Q_p(0^+)$
$t_s = \tau_p \ln(1 + \frac{I_F}{I_R})$
$I_{F} \searrow, I_{R} \nearrow t_{s} \searrow$
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