

## سوال 1 تمرین‌های کلاس تمرین

(الف)

$$\int_{-\infty}^{\infty} \delta(\alpha x) dx = \int_{-\infty}^{\infty} \delta(u) \frac{du}{|\alpha|} = \frac{1}{|\alpha|}$$

and so

$$\delta(\alpha x) = \frac{\delta(x)}{|\alpha|}.$$

Let  $x = \sqrt{u}$ , so  $dx = \frac{du}{2\sqrt{u}}$ , then

$$\int_0^{\infty} f(x) \delta(x^2 - a^2) dx = \int_0^{\infty} \frac{f(\sqrt{u})}{2\sqrt{u}} \delta(u - a^2) du = \frac{f(|a|)}{2|a|}.$$

Let  $x = -\sqrt{u}$ , so  $dx = -\frac{du}{2\sqrt{u}}$ , then

$$\int_{-\infty}^0 f(x) \delta(x^2 - a^2) dx = \int_0^{\infty} \frac{f(-\sqrt{u})}{2\sqrt{u}} \delta(u - a^2) du = \frac{f(-|a|)}{2|a|}.$$

Hence

$$\int_{-\infty}^{\infty} f(x) \delta(x^2 - a^2) dx = \frac{1}{2|a|} (f(|a|) + f(-|a|)) = \frac{1}{2|a|} (f(a) + f(-a)).$$

## سوال 1 تمرین‌های کلاس تمرین

(ج)

$$I = \int_{-\infty}^{\infty} t\delta'(t)dt = t\delta(t)|_{-\infty}^{\infty} - \int_{-\infty}^{\infty} \delta(t)dt = - \int_{-\infty}^{\infty} \delta(t)dt = \int_{-\infty}^{\infty} (-\delta(t))dt$$

$$\Rightarrow t\delta'(t) = -\delta(t)$$

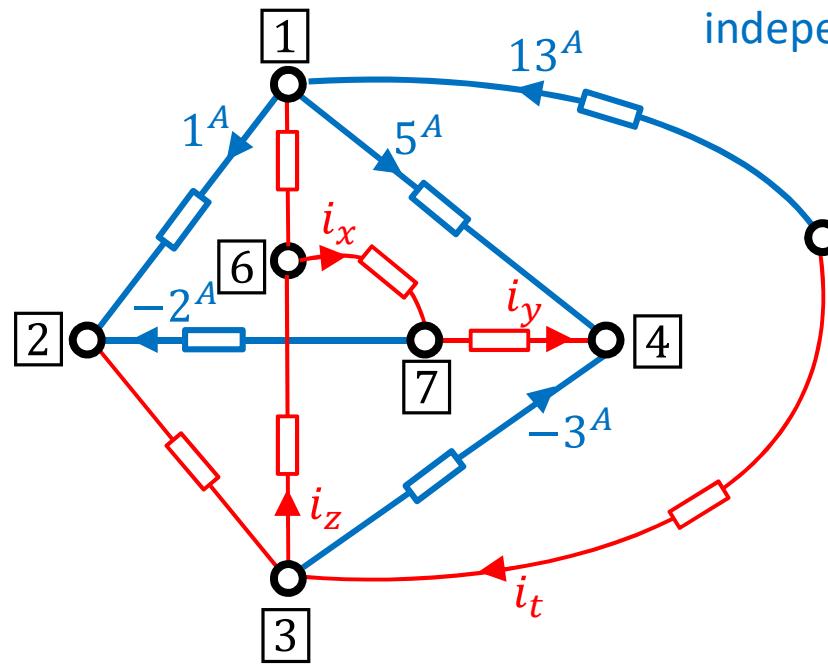
Hint:  $f(x) = x$ ,  $x_0 = 0$ ,  $\int_{-\infty}^{\infty} f(x)\delta(x-x_0)dx = f(x_0) \Rightarrow \int_{-\infty}^{\infty} x\delta(x)dx = 0 \Rightarrow t\delta(t) = 0$

(د)

$$I = \int_{-\infty}^{\infty} f(x)\delta'(x)dx = f(x)\delta(x)|_{-\infty}^{\infty} - \int_{-\infty}^{\infty} f'(x)\delta(x)dx = -f'(0)$$

Hint:  $f(x) = 0$  for  $|x| < b$  and  $x_0 = 0$ ,  $\int_{-\infty}^{\infty} f(x)\delta(x)dx = f(0) \Rightarrow \int_{-\infty}^{\infty} f(x)\delta(x)dx = 0$   
 So  $f(x)\delta(x) = 0$ .

١-الف



independent current variables

$$5: i_t = -13^A$$

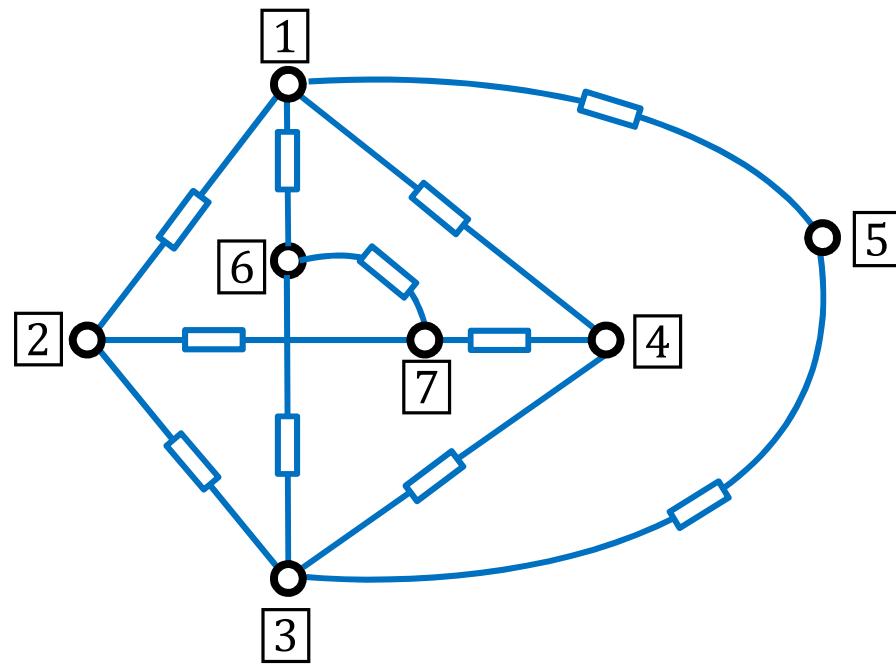
$$4: i_y = 3 - 5 = -2^A$$

$$7: i_x = -2 - 2 = -4^A$$

$$2: i_{2 \rightarrow 3} = 1 - 2 = -1^A$$

$$3: i_z = -13 + 3 - 1 = -11^A$$

۱-ب

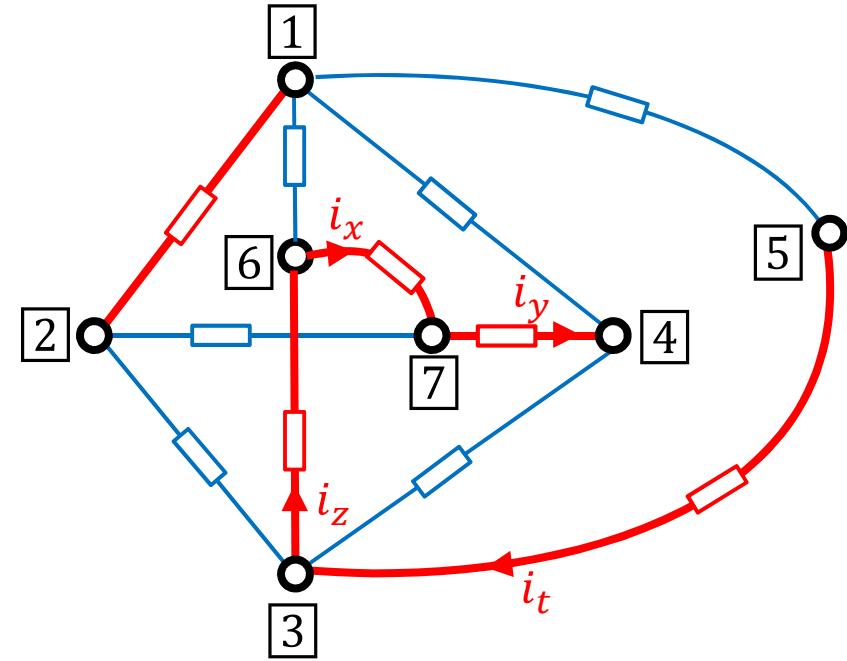
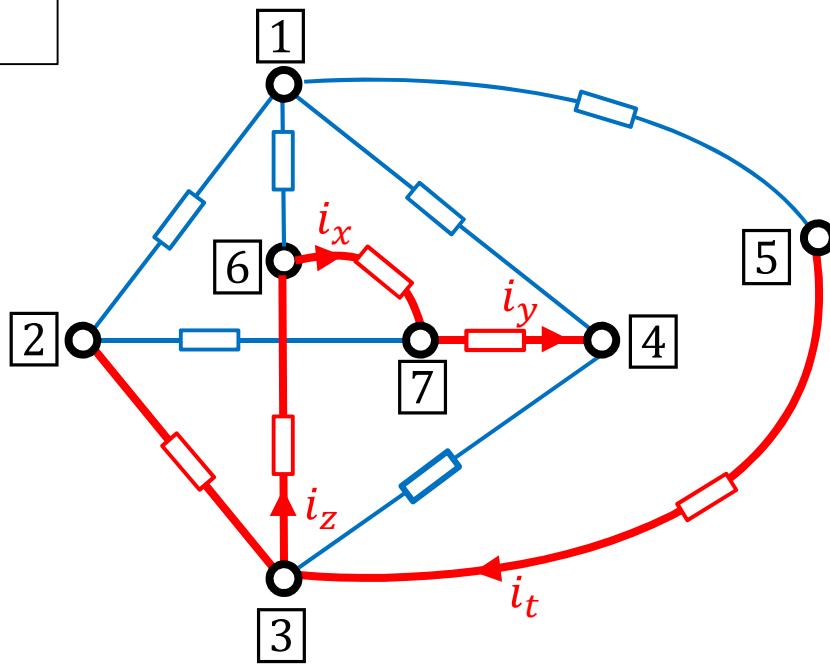


# of branches = 11  $\rightarrow$  # unknown currents = 11

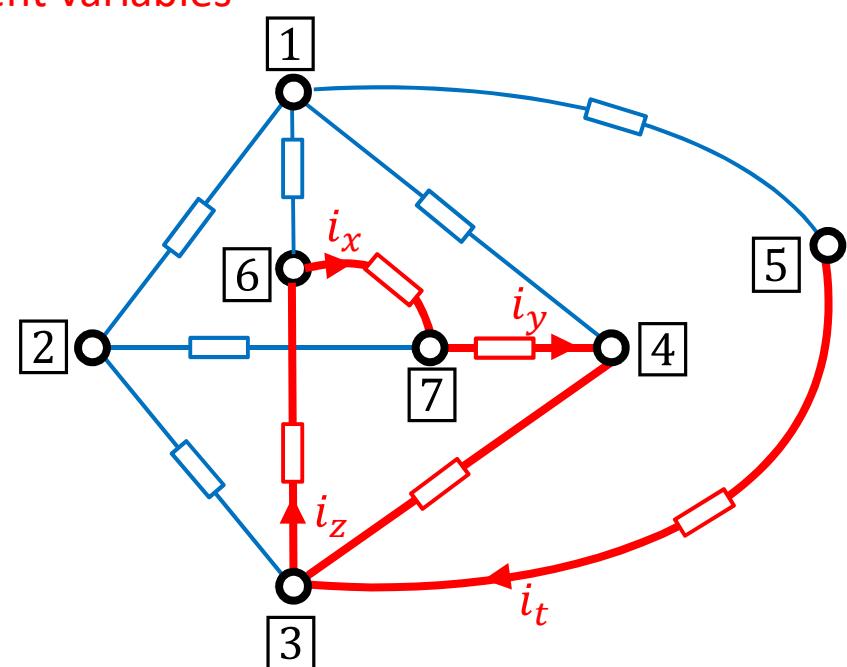
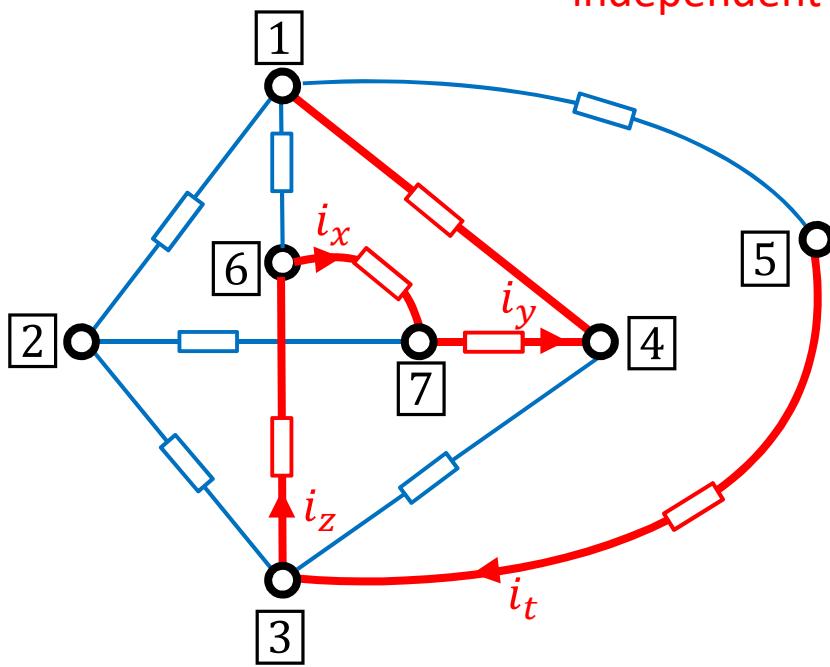
# of nodes = 7  $\rightarrow$  # independent KCL equations = 6

$\} \rightarrow$  # of independent current variables = 11 - 6 = 5

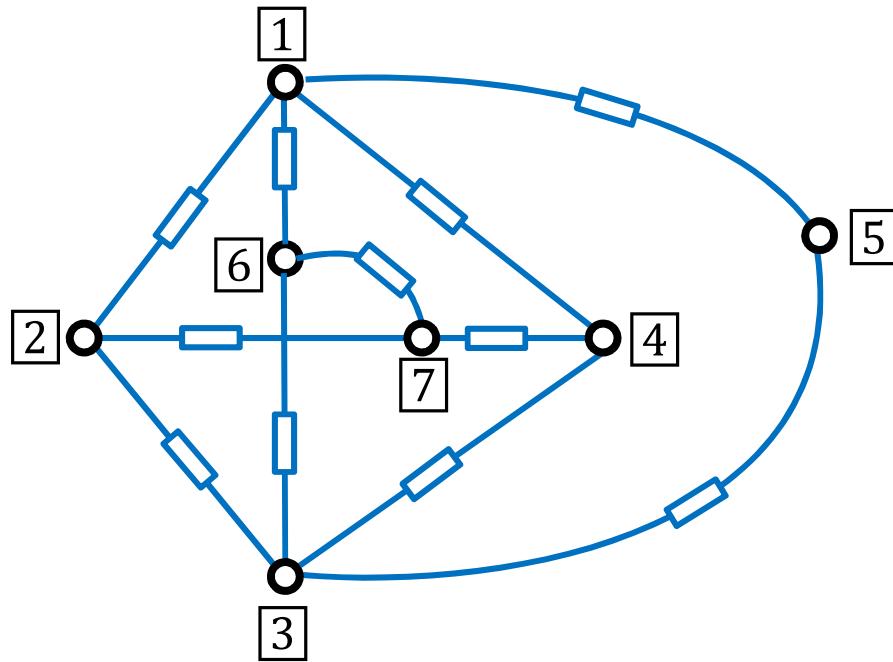
۱-۲



independent current variables



٢-الف



# unknown currents & voltages = 22

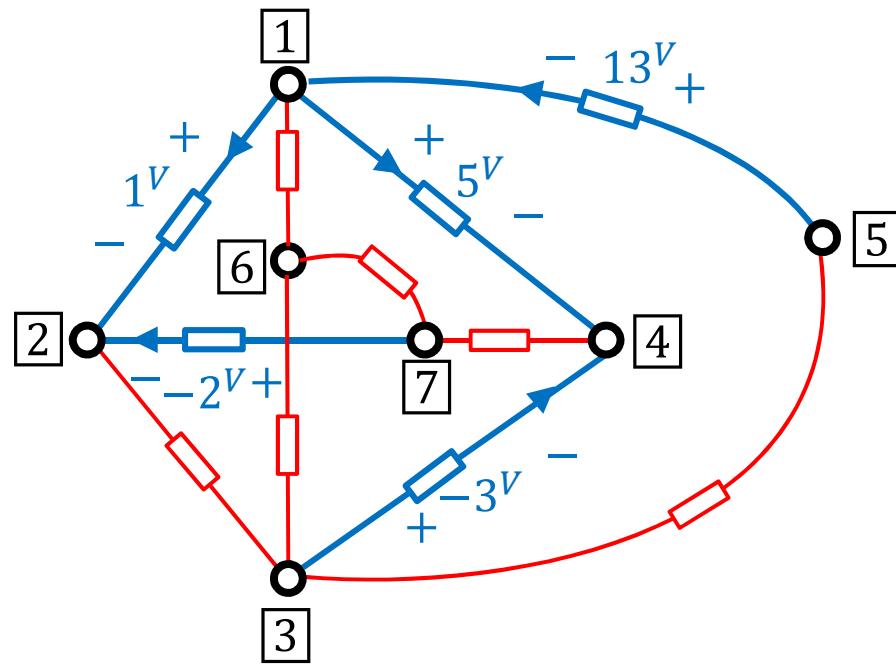
# independent KCL equations= 6

# equations for each branch= 11

→ # of independent voltage  
equations = $22-11-6= 5$

→ # of independent voltage variables = $11-5= 6$

ب-۲



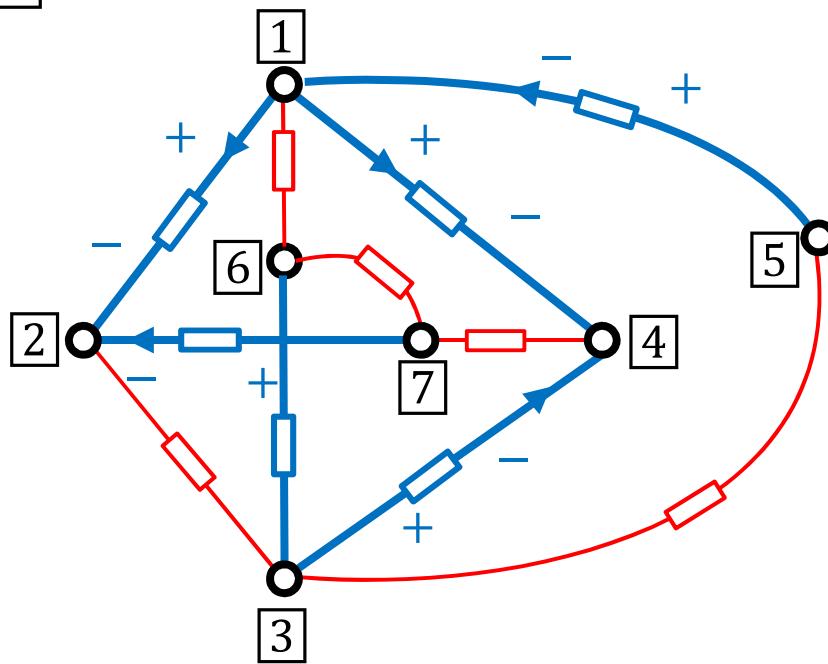
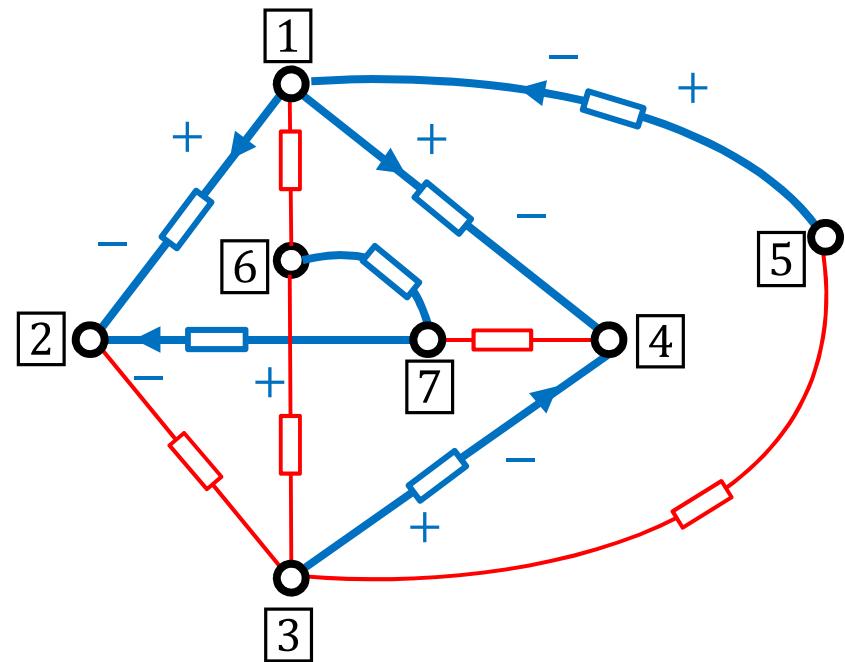
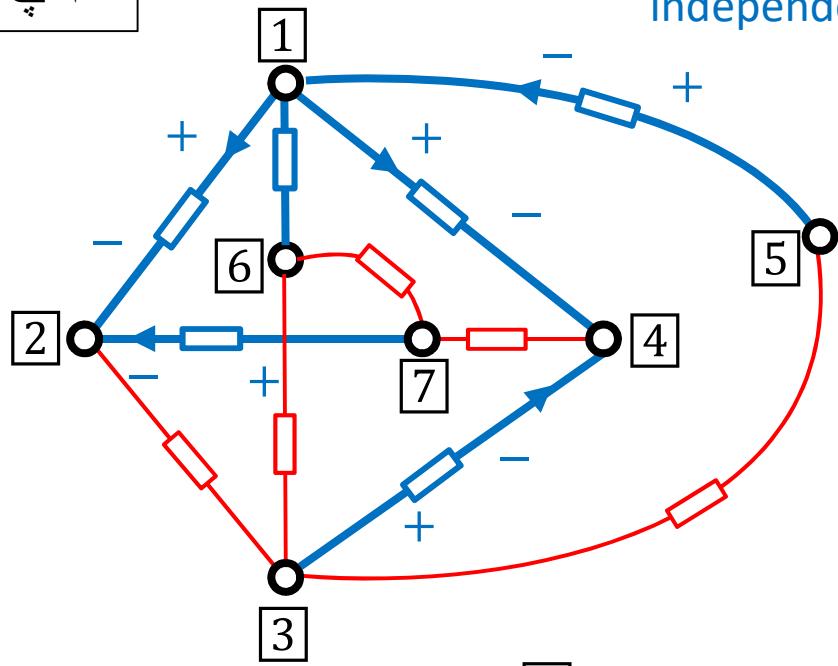
# independent voltage variables = 6

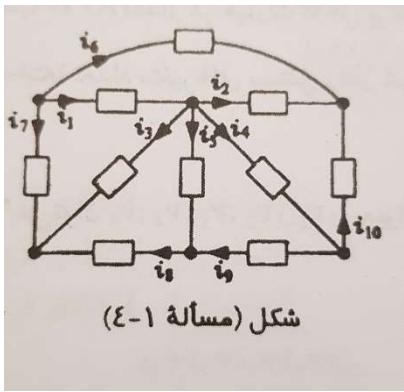
# given voltages = 5

→ unsolvable,  
1 more indep. voltage is needed

۲-۲

independent voltage variables





Subject.

Date.

سؤال ٤

الف)

$$\text{معادلة المقاومة} = 10 - V + 1 = \Delta$$

- ① :  $i_v + i_y + i_1 = 0$
- ② :  $i_t + i_x + i_5 - i_7 = 0$
- ③ :  $-i_t - i_y - i_{10} = 0$
- ④ :  $-i_v - i_t - i_x = 0$
- ⑤ :  $-i_{10} + i_y + i_8 = 0$

لـ أزمان نرجو جريان حاراً بحوالٍ متصلٍ درفت جريان ٤٢٣٢ بـ ٤٢٣١  
متصل بالـ ٤٢٣٢

$$i_5 = i_1 - i_3 - i_4$$

$$روابطها \quad i_v = -i_1 - i_4$$

$$\Rightarrow i_x = i_1 + i_2 - i_3$$

$$\text{جريان الماء} \quad i_9 = i_2 + i_3 + i_4$$

$$\text{جريان الماء المتصل} \quad i_{10} = -i_2 - i_4$$

$$V_{1,11} + V_{1,12} + \dots + V_{1,10} = 0 ?$$

بعض (٤٢٣٢)  $i_1, V_1, V_2, \dots, V_{10}$  مجهول

$$\Rightarrow \sum V_i = 0$$

بـ أنت بـ نجز مجهول مجهول في بايس ،

$$4 - 1 = 0$$

متصل  $V_1, V_2, V_3, V_4, V_5$

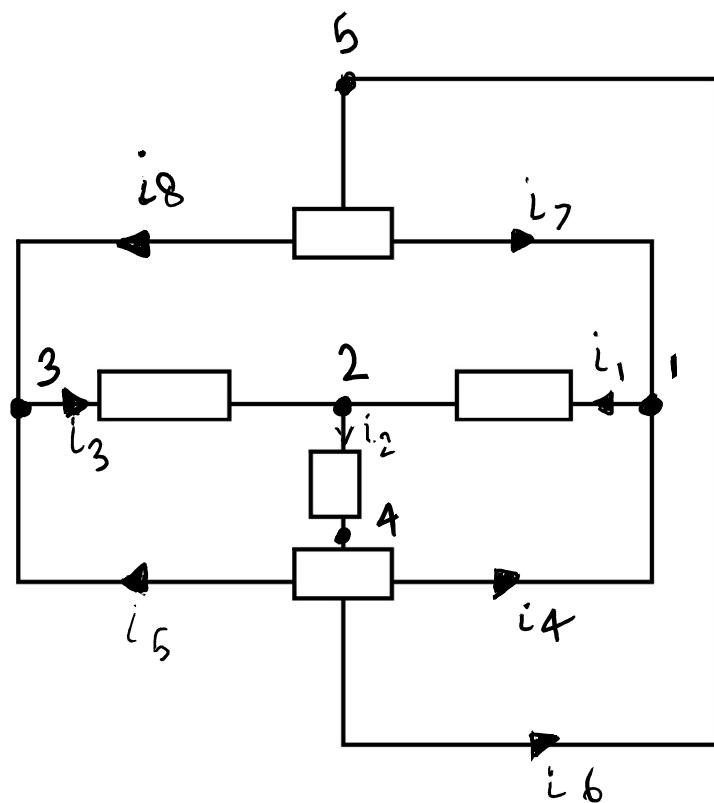
كـ رسو وـ رسو مجهولان !

$$\text{PAPCO} \quad \sum V_i = 0$$

11

/1

نکته این مساله این است که برای مدار های دارای عناصر سه سر یا ۴ سر مانند مدار های شامل عناصر دو سر قوانین kvl و kcl برقرار است.



kclها:

$$1) \quad i_4 + i_7 = i_1$$

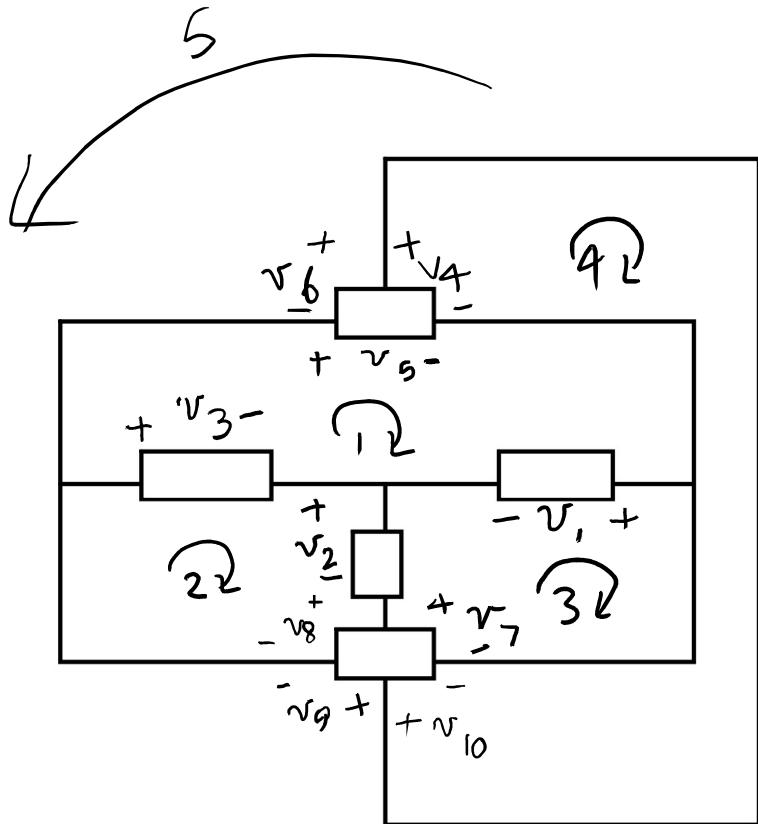
$$2) \quad i_1 + i_3 = i_2$$

$$3) \quad i_5 + i_8 = i_3$$

$$4) \quad i_4 + i_5 + i_6 = i_2$$

$$5) \quad i_7 + i_8 = i_6$$

11  
/2



lokvl:

$$1) -v_3 + v_S + v_1 = 0$$

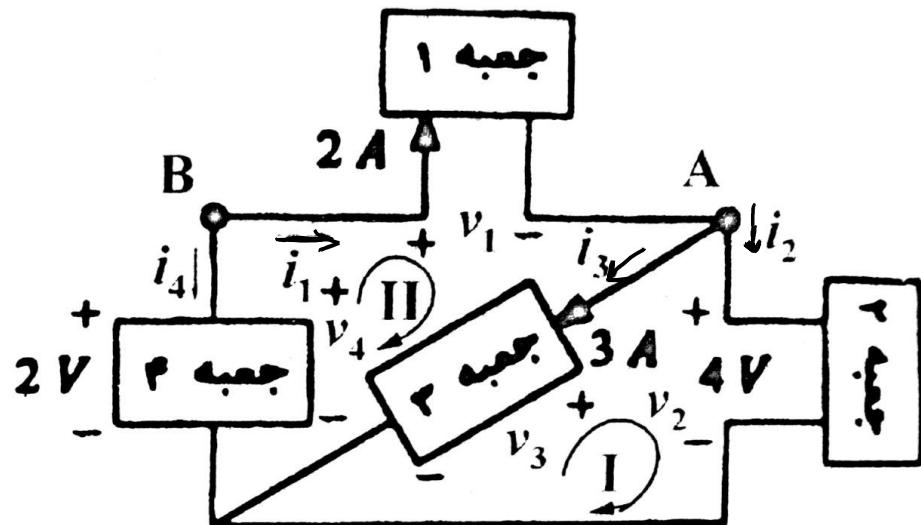
$$2) v_3 + v_2 + v_8 = 0$$

$$3) -v_7 - v_2 - v_1 = 0$$

$$4) -v_4 + v_{10} = 0$$

$$5) -v_9 + v_6 = 0$$

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$$KVL \text{ I}) V_2 - V_3 = 0 \Rightarrow \underline{V_3 = 4V}$$

$$KVL \text{ II}) V_1 + V_3 - V_4 = 0 \Rightarrow$$

$$\underline{V_1 = 2 - 4 = -2V}$$

$$KCL \text{ A}) i_1 = i_2 + i_3 \Rightarrow \underline{i_2 = -1A}$$

$$KCL \text{ B}) -i_1 = i_4 \Rightarrow \underline{i_4 = -2A}$$

$$P = Vi \Rightarrow \left\{ \begin{array}{l} P_1 = -2 \times 2 = -4W \\ P_2 = 4 \times -1 = -4W \\ P_3 = 4 \times 3 = 12W \\ P_4 = 2 \times -2 = -4W \end{array} \right.$$

$$\sum_{i=1}^4 P_i = -4 - 4 + 12 - 4 = 0$$

صوری از قضیه ملن برقرار است