



# Two Phase Flows

(Section 10)

## Pool Boiling

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# Assignment set 4

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Problems 6-11

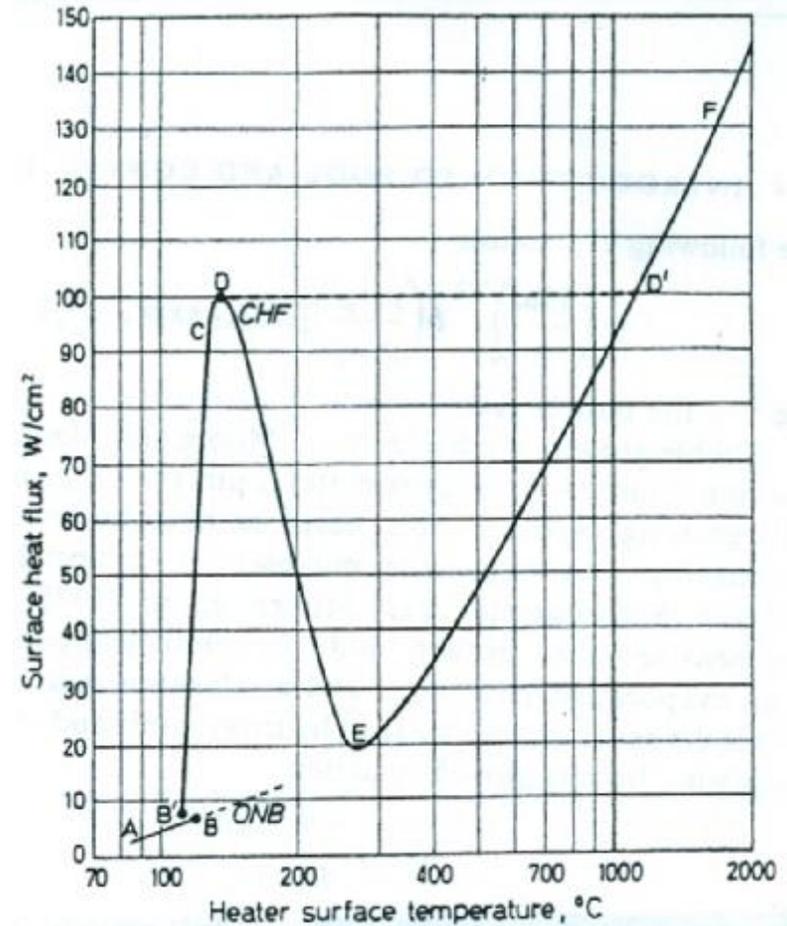
Chapter 2

Due to next Tuesday

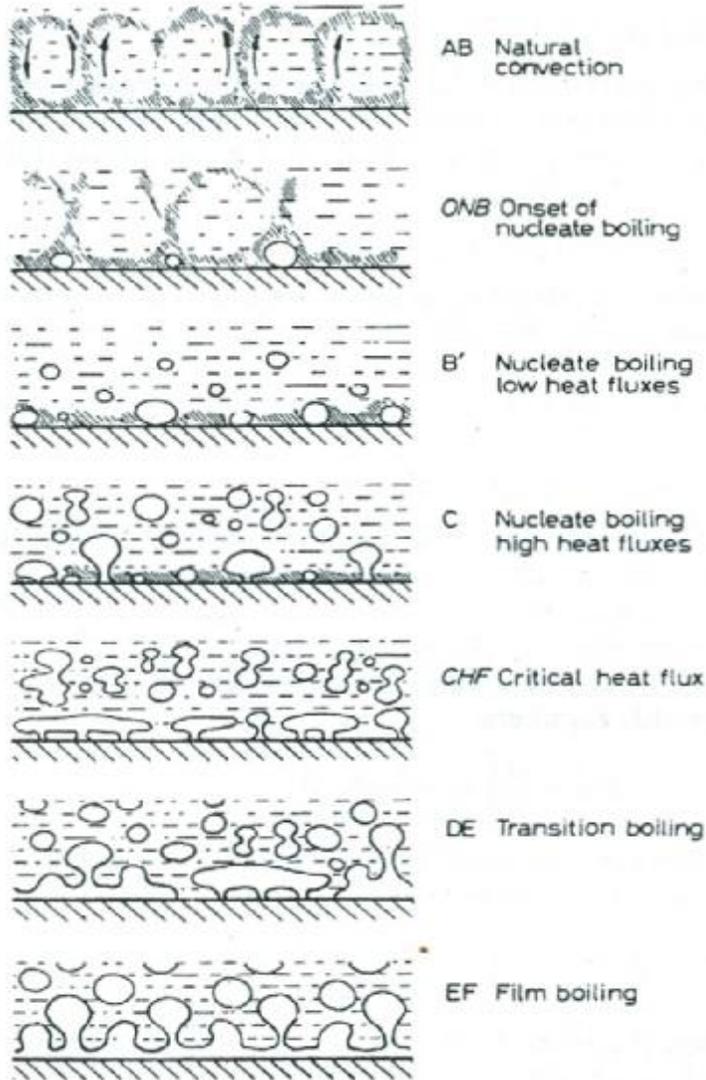
# Boiling curve



- AB Natural convection region
- AB-B'C Onset of Nucleate boiling
- B'C Nucleate boiling region
- D Critical heat flux
- DE transition boiling region
- EF film boiling region



# Various stages in boiling curve

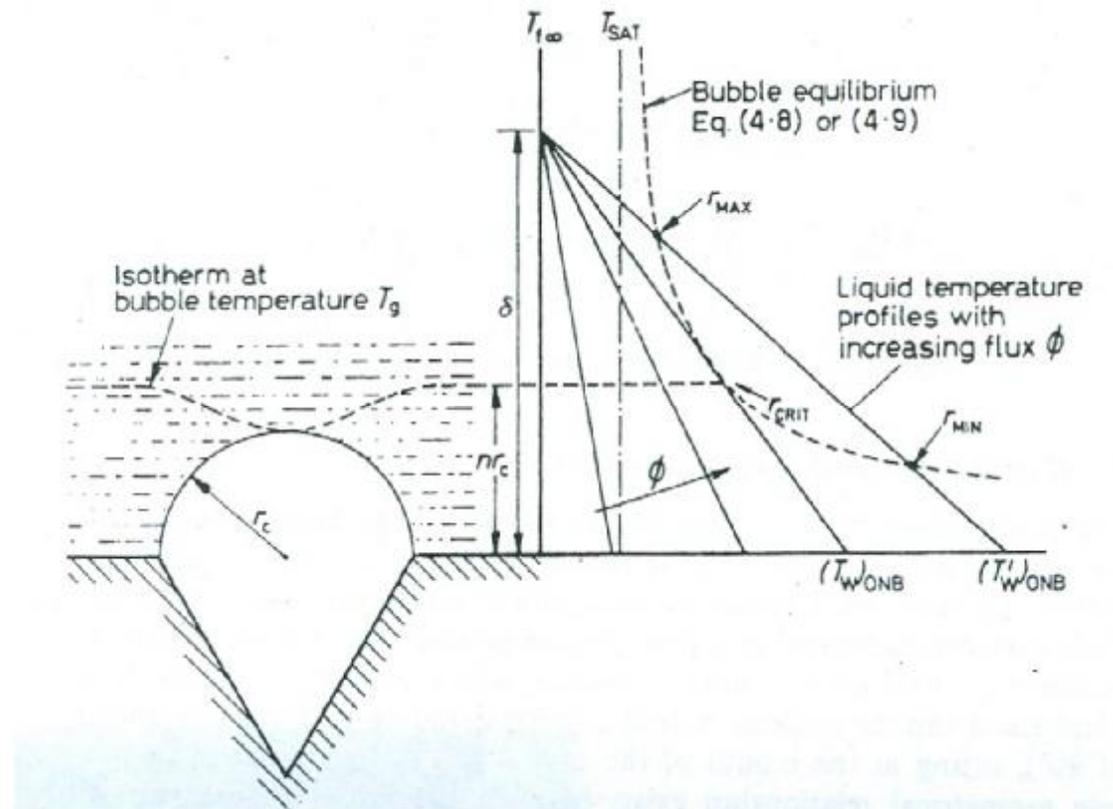


Natural Convection  
By: Fishenden and  
Saunders

$$\left[ \frac{hD}{k_f} \right] = 0.14 \left[ \left( \frac{b g \Delta T D^3 r_f^2}{m_f^2} \right) \left( \frac{c_p m}{k} \right)_f \right]^{1/3}$$

# ONB

Onset of Nucleation Boiling



# Nucleate Boiling Correlations

Power law relationship



$$T_W - T_{SAT} = y f^n$$

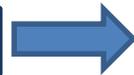
$$Nu = C_1 Re^x Pr^y$$

Using bubble dia. at departure as characteristic length



$$Nu = \frac{h}{k_f} \left[ \frac{s}{g(r_f - r_g)} \right]^{1/2}$$

Roshenow (1952)



$$Re = \frac{f}{i_{fg} r_f} \left[ \frac{s}{g(r_f - r_g)} \right]^{1/2} \frac{r_f}{m_f}$$



$$Nu = \frac{1}{C_{sf}} Re^{1-n} Pr_f^{-m}$$



$$\frac{c_{pf} \Delta T_{SAT}}{i_{fg}} = C_{sf} \left[ \frac{f}{i_{fg} r_f} \left( \left[ \frac{s}{g(r_f - r_g)} \right]^{1/2} \right) \right]^n \left[ \left( \frac{c_p m}{k} \right)_f \right]^{m+1}$$

# Nucleate Boiling Correlations

Forster and Zuber (1955)

$$\frac{f}{i_{fg} r_f} \left( \frac{p}{a_f} \right)^{1/2} \left[ \frac{r_f r^{*3}}{2s} \right]^{1/4} = 0.0015 \left[ \frac{r_f}{m_f} \left( \frac{\Delta T_{SAT} k_f}{i_{fg} r_f} \right)^2 \frac{p}{a_f} \right]^{5/8} \left[ \left( \frac{c_p m}{k} \right)_f \right]^{1/3}$$

Borishanski (1969)

$$h = A^* f^{0.7} F(p)$$

$$A^* = 0.1011 p_{cr}^{0.69}$$

$$F(p) = 1.8 p_r^{3.17} + 4 p_r^{1.2} + 10 p_r^{10}$$

Cooper (1984)

$$h = 55 p_r^{0.12 - 0.4343 \ln R_p} (-0.4343 \ln P_r)^{-0.55} M^{-0.5} f^{0.67}$$

# Nucleate Boiling Correlations



Gorenflo (1990, 1993)

$$h = h_0 F_{PF} \left[ \frac{f}{f_0} \right]^{nf} \left[ \frac{R_p}{R_{p0}} \right]^{0.133}$$

Water:

$$F_{PF} = 1.73 P_r^{0.27} + \left( 6.1 + \frac{0.68}{1 - P_r} \right) P_r^2$$

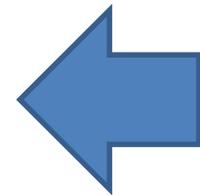
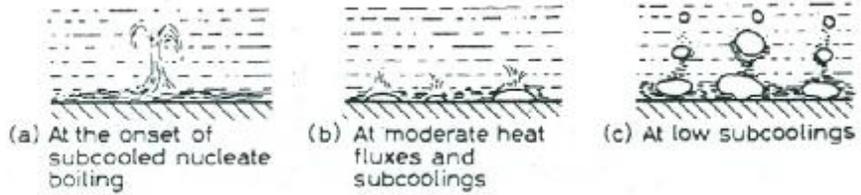
$$nf = 0.9 - 0.3 P_r^{0.15}$$

All fluids except water

$$F_{PF} = 1.2 P_r^{0.27} + 2.5 P_r + \frac{P_r}{1 - P_r}$$

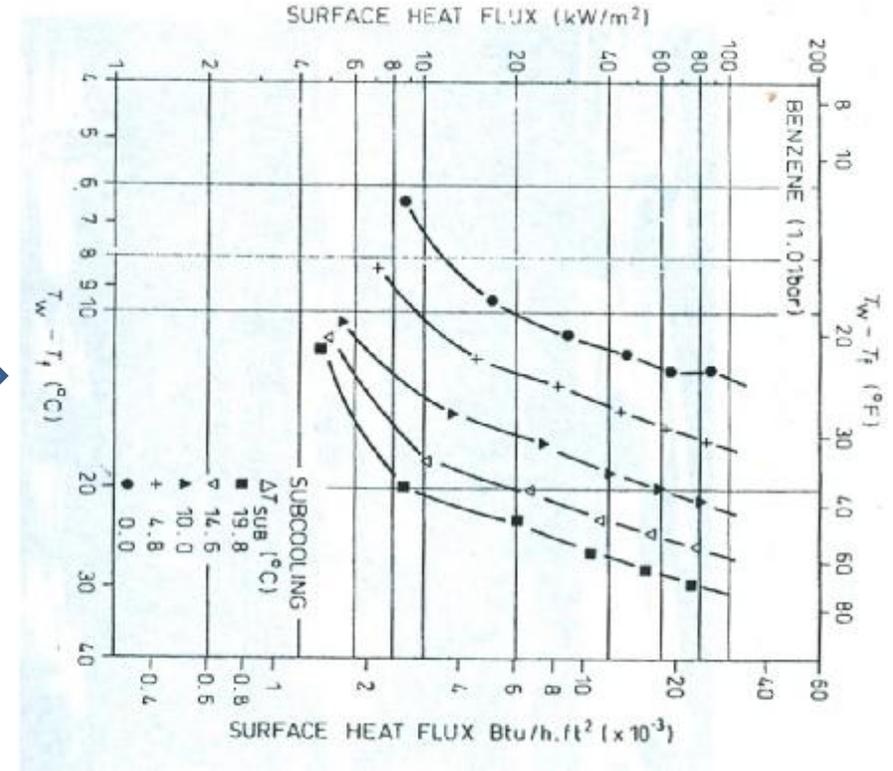
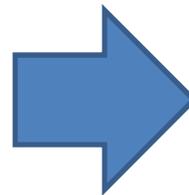
$$nf = 0.9 - 0.3 P_r^{0.3}$$

# Heat transfer Mechanism



Sub cooled nucleate boiling

Sub cooled boiling of benzene



# Heat transfer Mechanism

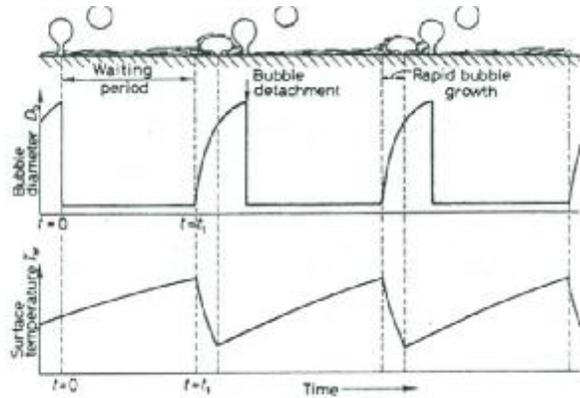
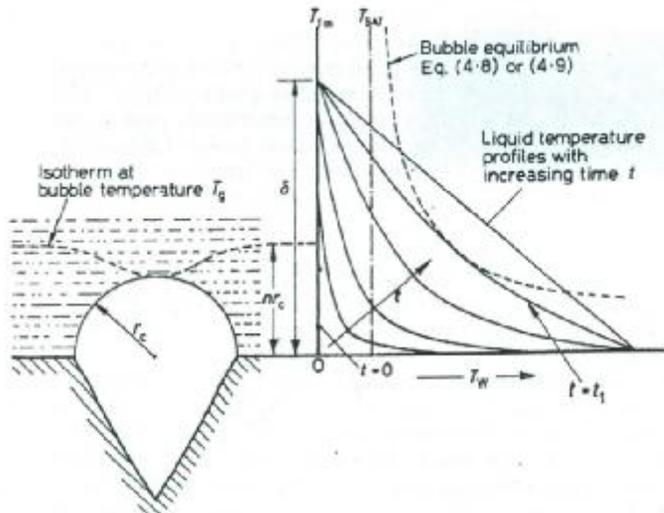


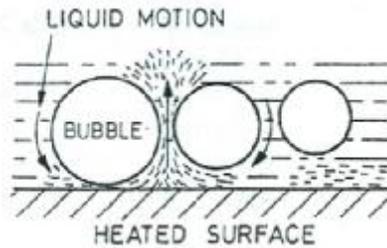
Fig. 4.16. Behaviour at a single nucleation site.

Behavior at a single nucleation site

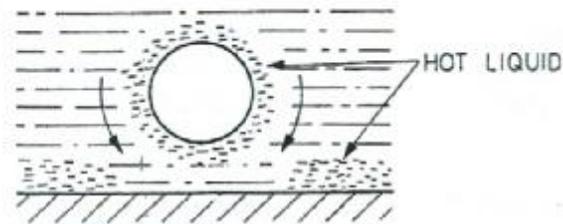


Waiting period

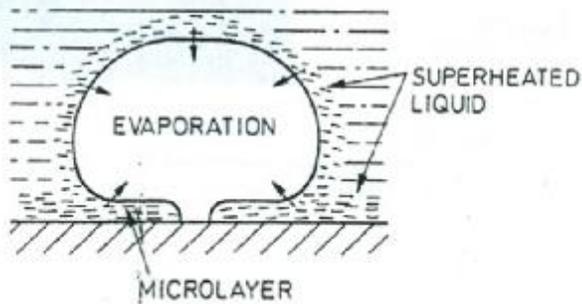
# Heat transfer Mechanism



Plain Surface nucleate boiling



1. Bubble agitation
2. Thermal boundary layer stripping
3. Evaporation

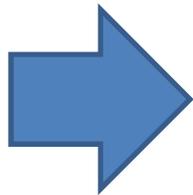


# Critical Heat Flux

Helmholtz instability limits

$$(j_g)_{\max} = \frac{p}{24} \left[ \frac{sg(r_f - r_g)}{r_g^2} \right]^{1/4}$$

plates



$$j_g = \frac{f}{i_{fg} r_f}$$

$$f_{CRIT} = Ki_{fg} r_g^{0.5} \left[ sg(r_f - r_g) \right]^{1/4}$$

$$\frac{f_{CRIT}}{(f_{CRIT})_{Zuber}} = fn(L')$$

Cylinders and spheres

Ivey and Morris (1986)

$$L' = 2p\sqrt{3} \frac{L}{l_d}$$

$$l_d = 2p\sqrt{3} \left[ \frac{s}{g(r_f - r_g)} \right]^{1/2}$$

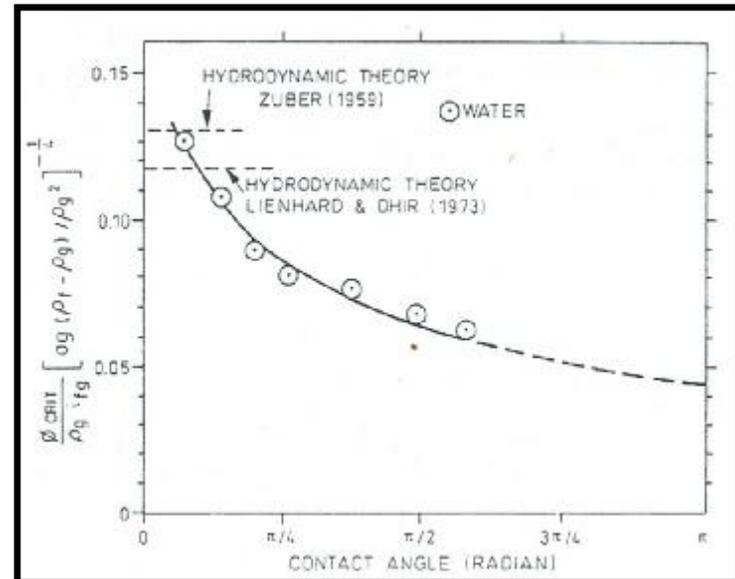
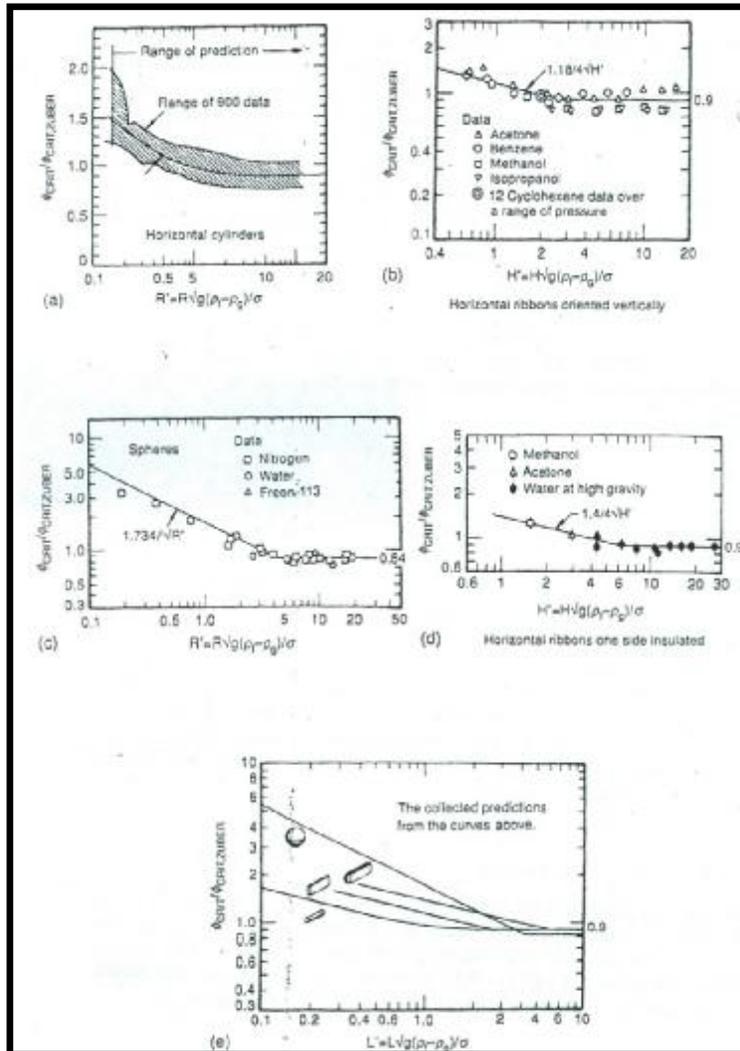
$$f_{CRIT} = Ki_{fg} r_g^{0.5} \left[ sg(r_f - r_g) \right]^{1/4} [1 + B\Delta T_{SUB}]$$



# CHF

Critical pool boiling heat flux on several heaters

Dependence of CHF on contact angle



# Film boiling

Bromely (1950)

$$h = 0.62 \left[ \frac{g(r_f - r_g) r_g k_g^3 i'_{fg}}{D m_g \Delta T} \right]$$

where



$$i'_{fg} = i_{fg} \left[ 1 + 0.68 \left( \frac{c_{pg} \Delta T}{i_{fg}} \right) \right]$$

Berenson (1961)

$$h = 0.425 \left[ \frac{g(r_f - r_g) r_g k_g^3 i'_{fg}}{m_g \Delta T_{SAT} \left[ \frac{s}{g(r_f - r_g)} \right]^{1/2}} \right]^{1/4}$$

Considering radiation  
in high temperatures



$$h = h_c + 0.75h_r$$

$$h_r = se \left[ \frac{T_w^4 - T_f^4}{T_w - T_f} \right]$$